Learning Bayesian Networks from Data

—NIPS 2001 Tutorial—

Relevant Readings

The following is a list of references to the material covered in the tutorial and to more advanced subjects mentioned at various points. This list is far from being comprehensive and is intended only to provide useful starting points.

Background Material

Bayesian Networks   The seminal reference on Bayesian networks is [Pearl 1988]. A more recent book, which covers BN inference in more depth, as well as some of the recent developments in the area, is [Cowell et al. 1999]. A short and gentle introduction can be found in [Charniak 1991].

Statistics, Pattern Recognition and Information Theory   There are many books on statistics. We find [DeGroot 1970] to be a good introduction to statistics and Bayesian statistics in particular. A more recent book [Gelman et al. 1995] is also a good introduction to this field and also discusses recent advances, such as hierarchical priors. Books in pattern recognition, including the classic [Duda and Hart 1973] and the more recent [Bishop 1995], cover basic issues in density estimation and their use for pattern recognition and classification. A good introduction to information theory, and notions such as KL divergence and mutual information can be found in [Cover and Thomas 1991].

Tutorials and Surveys   [Heckerman 1998] provides an in-depth tutorial on Bayesian methods in learning Bayesian networks. [Buntine 1996] surveys the literature. [Jordan 1998] is a collection of introductory surveys and papers discussing recent advances.

Parameter Estimation

Learning parameters from complete data is discussed in [Spiegelhalter and Lauritzen 1990]. A more recent discussion can be found in [Buntine 1994].

Model Selection

The Bayesian score is originally discussed in [Cooper and Herskovits 1992] and further developed in [Buntine 1991; Heckerman et al. 1995]. The MDL score is based on the Minimal Description Length principle of [Rissanen 1989]; the application of this principle to Bayesian networks was developed by several authors [Bouckaert 1994; Lam and Bacchus 1994a; Suzuki 1993]. The method for learning trees was initially introduced in [Chow and Liu 1968] (see also the description in [Pearl 1988]). Learning structure using greedy hill-climbing and other variants is discussed and evaluated in [Heckerman et al. 1995]. [Moore and Lee 1997] describe methods for efficiently collecting sufficient statistics from datasets with large number of instances. [Friedman et al. 1999] discuss efficient heuristic algorithms for learning with many variables. See [Chickering 1995] for search over equivalence network classes.

Structure Discovery

Several papers discuss the idea of doing structure discovery by approximating the full Bayesian model averaging. [Buntine 1991; Heckerman et al. 1995] discuss special cases where a full enumeration of models is possible. [Madigan and Raftery 1994] propose a heuristic approximation that restricts attention to only a subset of models. [Madigan and York 1995; Madigan et al. 1996; Giudici and Green 1999; Giudici et al. 2000] discuss the use of a Markov chain over the set of structures. [Friedman and Koller 2001] introduce the idea of a Markov chain over orderings. Recently, [Heckerman et al. 2000] discuss dependency networks that are similar to Bayesian networks and can capture properties of dependencies among variables.

Incomplete Data

Parameter Estimation   An introduction to the possible problems with incomplete data and MAR assumptions can be found in [Rubin 1976]. Learning parameters from incomplete data using gradient methods is discussed by [Binder et al. 1997; Thiesson 1995]. The original EM paper is [Dempster et al. 1977]; an elegant alternative explanation of EM can found in [Neal and Hinton 1998]. [Lauritzen 1995] describes how to apply EM to Bayesian networks. [Bauer et al. 1997] describe methods for accelerating the convergence of EM. Learning using Gibbs sampling is discussed in [Gilks et al. 1996].

Model Selection   [Chickering and Heckerman 1997] discuss the problems with evaluating the score of networks in the presence of incomplete data and describe several approximation to the score. [Geiger et al. 1996; Geiger and Meek 1998] present more detailed analysis of statistical properties of these scores. [Cheeseman and Stutz 1995] discuss Bayesian learning of mixture models with a single hidden variable. The structural EM approach was introduced in [Friedman 1997; Friedman 1998]. Other papers on structure learning with incomplete data include [Meila and Jordan 1998; Singh 1997; Thiesson et al. 1998].

Advanced Topics

Causal Discovery   For different views of the relation of causality and Bayesian networks see [Spirtes et al. 1993; Heckerman and Shachter 1994; Pearl 2000]. [Pearl and Verma 1991; Spirtes et al. 1993] describe constraint-based methods for learning causal relation from data. The Bayesian approach is discussed in [Heckerman et al. 1997]. [Cooper and Glymour 1999] is a recent collection that discusses advanced issues in causal discovery.

Continuous Variables   See [Heckerman and Geiger 1995] for methods of learning a network that contains Gaussian distributions. [Hofmann and Tresp 1996; John and Langley 1995] discuss learning Bayesian networks with non-parametric representations of density functions. [Monti and Cooper 1997] use neural networks to represent the conditional densities. [Friedman and Goldszmidt 1996; Monti and Cooper 1998] learn Bayesian networks over continuous domains by discretizing the values of the continuous variables.

Learning Local Structure   [Buntine 1991; Diez 1993] discuss learning the "noisy-or" conditional probability. [Meek and Heckerman 1997] discuss how to learn a several extensions of this local model. [Friedman and Goldszmidt 1998] describe how to learn tree-like representations of local structure and why this helps in learning global structure. [Chickering et al. 1997] extend these results to richer representations and discuss more advanced search procedures for learning both global and local structure.

Online & Active Learning   See [Neal and Hinton 1998; Bauer et al. 1997] for discussion on online parameter estimation for incomplete data, and [Buntine 1991; Friedman and Goldszmidt 1997; Lam and Bacchus 1994b] for sequential update of the structure as more data becomes available. *Active learning* is a general framework where the learner can select additional samples that will best allow it to refine its learned model. [Tong and Koller 2001a] describes active learning for Bayesian networks with a fixed structure. [Tong and Koller 2001b] describes active learning for structure discovery.

Temporal Processes   *Dynamic Bayesian networks* [Dean and Kanazawa 1989] is an extension of Bayesian networks for representing stochastic models. [Smyth et al. 1997] discussed how this representation generalizes hidden Markov networks, and how methods from both fields are related. [Ghahramani and Jordan 1997] describe methods for learning parameters for complex dynamic Bayesian networks with non-trivial unobserved state. [Friedman et al. 1998] describe methods for learning the structure of dynamic Bayesian networks.

Incomplete Data in Intractable Networks   A major obstacle for learning with incomplete data requires using inference. In complex networks this might be intractable. In recent years there have been much progress on using of

approximate inference algorithms [Jordan et al. 1998; Murphy and Weiss 1999] for learning. For example, [Ghahramani and Jordan 1997] use EM-like algorithm to maximize the variational approximation lower-bound of the likelihood function. More recently, [Attias 1999; Ghahramani and Beal 2001] show how to use variational approximation directly for Bayesian inference.

Hidden Variables   [Elidan et al. 2001; Boyen et al. 1999] describe techniques for discovering a hidden variable from structural signatures in the learned model. [Elidan and Friedman 2001] describe a heuristic technique for picking the number of values for a hidden variable.

Probabilistic Relational Models   *Probabilistic relational models* [Koller and Pfeffer 1998] extend Bayesian networks to structured (relational) data. The basic framework for learning PRMs (parameters and structure) from data was discussed in [Friedman et al. 1999]. [Taskar et al. 2001] shows how to deal with incomplete data in PRMs, and applies the framework to relational classification and clustering. [Getoor et al. 2001] shows how to learn PRMs which also include a probabilistic model about the presence of links.

Theory   [Chickering 1996] shows that finding the structure that maximizes the Bayesian score is NP-hard. [Dasgupta 1999] shows that learning polytrees (singly connected Bayesian networks) is also NP-hard. [Dasgupta 1997; Friedman and Yakhini 1996] discuss the *sample complexity*—that is, how many examples are required to achieve a desired accuracy—for learning parameters and structure.

Applications

The AutoClass system [Cheeseman and Stutz 1995] is an unsupervised clustering program that the simple "naive" Bayesian network. This program has been used in numerous applications. The "naive" Bayesian classifier has been used since the early days of pattern recognition [Duda and Hart 1973]. [Ezawa and Schuermann 1995; Friedman et al. 1997; Singh and Provan 1995] describe applications of more complex Bayesian network learning algorithms for classification. [Zweig and Russell 1998] use Bayesian networks for speech recognition. [Breese et al. 1998] discuss collaborative filtering methods that use Bayesian network learning algorithms. [Spirtes et al. 1993] describe several applications of causal learning in social sciences. [Heckerman et al. 2000] discuss application of dependency networks for data visualization. [Friedman et al. 2000; Pe'er et al. 2001] discuss application of structure discovery for gene expression data. The application of structural EM to phylogenetics is described in [Friedman et al. 2001]. [Segal et al. 2001] describes the application of probabilistic relational models to the analysis of gene microarray data.

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