

## Query Optimization

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## Why Optimize?

- Given a query of size  $n$  and a database of size  $m$ , how big can the output of applying the query to the database be?
  - Example:  $R(A)$  with 2 rows. One row has value 0. One row has value 1.
    - How many rows are in  $R \times R$ ?
    - How many in  $R \times R \times R$ ?
- Size of output as a function of input:  $O(?)$

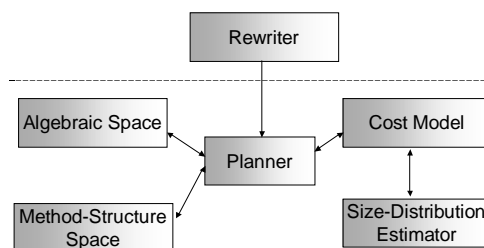
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## Data Complexity

- Usually, queries are small. Therefore, it is usually assumed that queries are of a fixed size.
- Use term **Data Complexity** when we analyze time, assuming that query is constant
- What is the size of the output in this case?

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## Optimizer Architecture



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## Optimizer Architecture

- **Rewriter**: Finds equivalent queries that, perhaps can be computed more efficiently. All such queries are passed on to the Planner.
  - Examples of Equivalent queries: Join orderings
- **Planner**: Examines all possible execution plans and chooses the cheapest one, i.e., fastest one.
  - Uses other modules to find best plan.

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## Optimizer Architecture (cont.)

- **Algebraic Space**: Determines which types of queries will be examined.
  - Example: Try to avoid Cartesian Products
- **Method-Space Structure**: Determines what types of indexes are available and what types of algorithms for algebraic operations can be used.
  - Example: Which types of join algorithms can be used

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### Optimizer Architecture (cont.)

- **Cost Model:** Estimates the cost of execution plans.
  - Uses Size-Distribution Estimator for this.
- **Size-Distribution Estimator:** Estimates size of tables, intermediate results, frequency distribution of attributes and size of indexes.

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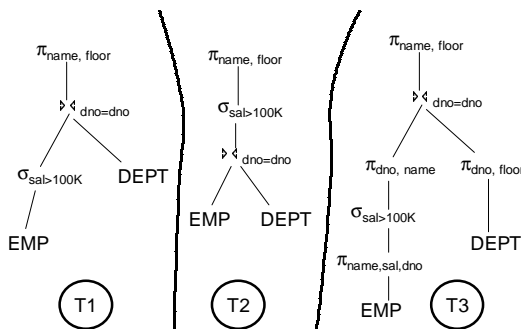
### Algebraic Space

- We consider queries that consist of select, project and join. (Cartesian product is a special case of join.)
- Such queries can be represented by a tree.
- Example: emp(name, age, sal, dno)  
dept(dno, dname, floor, mgr, ano)  
act(ano, type, balance, bno)  
bank(bno, bname, address)

```
select name, floor
from emp, dept
where emp.dno=dept.dno and sal>100K
```

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### 3 Trees



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### Restriction 1 of Algebraic Space

- Algebraic space may contain many equivalent queries
- Important to restrict space - Why?
- **Restriction 1:** Only allow queries for which selection and projection:
  - are processed as early as possible
  - are processed on the fly
- Which trees in our example conform to Restriction 1?

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### Performing Selection and Projection "On the Fly"

- Selection and projection are performed as part of other actions
- Projection and selection that appear one after another are performed one immediately after another
- ➔ Projection and Selection do not require writing to the disk
- Selection is performed while reading relations for the first time
- Projection is performed while computing answers from previous action

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### Processing Selection/Projection as Early as Possible

- The three trees differ in the way that selection and projection are performed
- In T3, there is "maximal pushing of selection and projection"
  - Rewriter finds such expressions
- Why is it good to push selection and projection?

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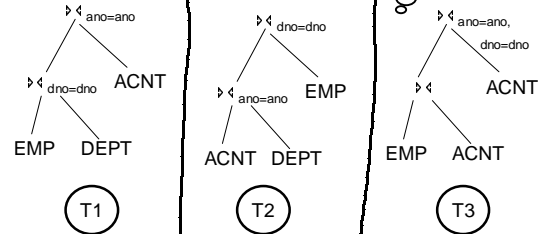
### Restriction 2 of Algebraic Space

- Since the order of selection and projection is determined, we can write trees only with joins.
- **Restriction 2:** Cross products are never formed, unless the query asks for them.
- Why this restriction?
- Example:

```
select name, floor, balance
from emp, dept, acct
where emp.dno=dept.dno and
dept.ano = acct.ano
```

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### 3 Trees



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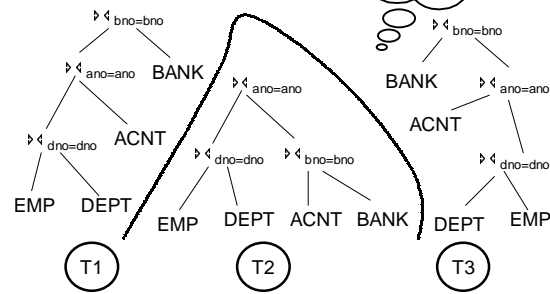
### Restriction 3 of Algebraic Space

- The left relation is called the outer relation in a join and the right relation is the inner relation. (as in terminology of nested loops algorithms)
- **Restriction 3:** The inner operand of each join is a database relation, not an intermediate result.
- Example:

```
select name, floor, balance
from emp, dept, acct, bank
where emp.dno=dept.dno and dept.ano=acct.ano
and acct.bno = bank.bno
```

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### 3 Trees



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### Algebraic Space - Summary

- We allow plans that
  1. Perform selection and projection early and *on the fly*
  2. Do not create cross products
  3. Use database relations as inner relations (also called left-deep trees)

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### Planner

- Dynamic programming algorithm to find best plan for performing join of  $N$  relations.
- Intuition:
  - Find all ways to access a single relation. Estimate costs and choose best access plan(s)
  - For each pair of relations, consider all ways to compute joins using all access plans from previous step. Choose best plan(s)...
  - For each  $i-1$  relations joined, find best option to extend to  $i$  relations being joined...
  - Given all plans to compute join of  $n$  relations, output the best.

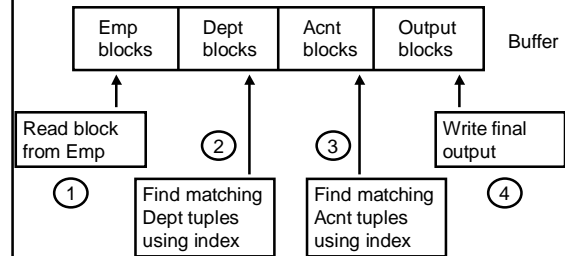
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### Pipelining Joins

- Consider computing:  $(Emp \bowtie Dept) \bowtie Acnt$ . In principle, we should
  - compute  $Emp \bowtie Dept$ , write the result to the disk
  - then read it from the disk to join it with  $Acnt$
- When using block and index nested loops join, we can avoid the step of writing to the disk.
- Do you understand now restriction 3?

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### Pipelining Joins - Example



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### Reminder: Dynamic Programming

- To find an optimal plan for joining  $R_1, R_2, R_3, R_4$ , choose the best among:
  - Optimal plan for joining  $R_2, R_3, R_4$  + for reading  $R_1$  + optimal join of  $R_1$  with result of previous joins
  - Optimal plan for joining  $R_1, R_3, R_4$  + for reading  $R_2$  + optimal join of  $R_2$  with result of previous joins
  - Optimal plan for joining  $R_1, R_2, R_4$  + for reading  $R_3$  + optimal join of  $R_3$  with result of previous joins
  - Optimal plan for joining  $R_1, R_2, R_3$  + for reading  $R_4$  + optimal join of  $R_4$  with result of previous joins

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### Not Good Enough

- Example, suppose we are computing  $(R(A,B) \bowtie S(B,C)) \bowtie T(B,D)$
- Maybe merge-sort join of  $R$  and  $S$  is not the most efficient, but the result is sorted on  $B$
- If  $T$  is sorted on  $B$ , the performing a sort-merge join of  $R$  and  $S$ , and then of the result with  $T$ , maybe the cheapest total plan

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### Interesting Orders

- For some joins, such as sort-merge join, the cost is cheaper if relations are ordered
- Therefore, it is of interest to create plans where attributes that participate in a join are ordered on attributes in joins later on
- For each *interesting order*, save the best plan.
- We save plans for non order if it better than all interesting order costs

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### Example

- We want to compute the query:

```
select name, mgr
from emp, dept
where emp.dno=dept.dno and sal>30K and floor = 2
```

- Available Indexes: B+tree index on  $emp.sal$ , B+tree index on  $emp.dno$ , hashing index on  $dept.floor$
- Join Methods: Block nested loops, index nested loops and sort-merge
- In the example, all cost estimations are fictional.

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### Step 1 - Accessing Single Relations

Relation	Interesting Order	Plan	Cost
emp	emp.dno	Access through B+tree on emp.dno	700
		Access through B+tree on emp.sal	200
		Sequential scan	600
dept		Access through hashing on dept.floor	50
		Sequential scan	200

Which do we save for the next step?

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### Step 2 - Joining 2 Relations

Join Method	Outer/Inner	Plan	Cost
nested loops	empt/dno	For each emp tuple obtained through B+Tree on emp.sal, scan dept through hashing index on dept.floor to find tuples matching on dno	1800
		For each emp tuple obtained through B+Tree on emp.dno and satisfying selection, scan dept through hashing index on dept.floor to find tuples matching on dno	3000

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### Step 2 - Joining 2 Relations

Join Method	Outer/Inner	Plan	Cost
nested loops	dept/emp	For each dept tuple obtained through hashing index on dept.floor, scan emp through B+Tree on emp.sal to find tuples matching on dno	2500
		For each dept tuple obtained through hashing index on dept.floor, scan emp through B+Tree on emp.dno to find tuples satisfying the selection on emp.sal	1500

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### Step 2 - Joining 2 Relations

Join Method	Outer/Inner	Plan	Cost
sort merge		Sort the emp tuples resulting from accessing the B+Tree on emp.sal into L1 Sort the dept tuples resulting from accessing the hashing index on dept.floor into L2 Merge L1 and L2	2300
		Sort the dept tuples resulting from accessing the hashing index on dept.floor into L2 Merge L2 and the emp tuples resulting from accessing the B+Tree on emp.dno and satisfying the selection on emp.sal	2000

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### The Plan

- Which plan will be chosen?

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### Cost Model

- Taught In class: estimate time of computing joins
- Now: Estimating result size

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## Estimating Result Sizes

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## Picking a Query Plan

- Suppose we want to find the natural join of: Reserves, Sailors, Boats.
- The 2 options that appear the best are (ignoring the order within a single join):

(Sailors  $\bowtie$  Reserves)  $\bowtie$  Boats

Sailors  $\bowtie$  (Reserves  $\bowtie$  Boats)

- We would like intermediate results to be as small as possible. Which is better?

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## Analyzing Result Sizes

- In order to answer the question in the previous slide, we must be able to estimate the size of (Sailors  $\bowtie$  Reserves) and (Reserves  $\bowtie$  Boats).
- The DBMS stores statistics about the relations and indexes.
- They are updated periodically (*not* every time the underlying relations are modified).

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## Statistics Maintained by DBMS

- **Cardinality:** Number of tuples  $NTuples(R)$  in each relation  $R$
- **Size:** Number of pages  $NPages(R)$  in each relation  $R$
- **Index Cardinality:** Number of distinct key values  $NKeys(I)$  for each index  $I$
- **Index Size:** Number of pages  $INPages(I)$  in each index  $I$
- **Index Height:** Number of non-leaf levels  $IHeight(I)$  in each B+ Tree index  $I$
- **Index Range:** The minimum  $ILow(I)$  and maximum value  $IHigh(I)$  for each index  $I$

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## Estimating Result Sizes

- Consider

```
SELECT attribute-list
FROM relation-list
WHERE term1 and ... and termn
```

- The maximum number of tuples is the product of the cardinalities of the relations in the FROM clause
- The WHERE clause is associating a **reduction factor** with each term
- Estimated result size is: maximum size times product of reduction factors

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## Estimating Reduction Factors

- **column = value:**  $1/NKeys(I)$  if there is an index  $I$  on *column*. This assumes a uniform distribution. Otherwise, System R assumes  $1/10$ .
- **column1 = column2:**  $1/\text{Max}(NKeys(I1), NKeys(I2))$  if there is an index  $I1$  on *column1* and  $I2$  on *column2*. If only one column has an index, we use it to estimate the value. Otherwise, use  $1/10$ .
- **column > value:**  $(\text{High}(I) - \text{value}) / (\text{High}(I) - \text{Low}(I))$  if there is an index  $I$  on *column*.

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### Example

```
SELECT *  
FROM Reserves R, Sailors S  
WHERE R.sid = S.sid and S.rating > 3 and  
R.agent = Joe
```

- Cardinality(R) = 1,000 \* 100 = 100,000
- Cardinality(S) = 500 \* 80 = 40,000
- NKeys(Index on R.agent) = 100
- High(Index on Rating) = 10, Low = 0

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### Example (cont.)

- Maximum cardinality: 100,000 \* 40,000
- Reduction factor of R.sid = S.sid: 1/40,000
- Reduction factor of S.rating > 3:  $(10-3)/(10-0) = 7/10$
- Reduction factor of R.agent = 'Joe': 1/100
- Total Estimated size: 700

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