# Data Structures – LECTURE 1

#### Introduction

- Motivation: algorithms and abstract data types
- Easy problems, hard problems
- Lecture and exercise topics
- Style of lectures and requirements

#### Programs and algorithms

- Why do we need algorithms?
   → to solve problems with a computing device
- What is the difference between an algorithm and a program?

→ a program is an *implementation* of an algorithm to be run on a specific computer and operating system. An algorithm is more abstract in that it does not deal with machine specific details – think of it as a *method* to solve a problem. The course emphasis is on algorithms.

#### Data structures

- A data structure is a method of storing data for the purpose of efficient computation
- → variables, arrays, linked lists, binary trees
  How data is stored is key for how a problem
- How data is stored is key for now a problem will be solved.
- Assumptions about the nature of the data determine what data structure and algorithm will be used → sorting integers vs. words
- Data structures and algorithm development go hand in hand! You cannot have one without the other!
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# Abstract Data Types – ADT

- An abstract data type is a collection of <u>formal</u> <u>specifications</u> of data-storing entities with a well designed set of operations.
- The set of operations defined with the ADT specification are the operations it "supports"
- What is the difference between a data structure (or a class of objects) and an ADT?

→ The data structure or class is an *implementation* of the ADT to be run on a specific computer and operating system. Think of it as an abstract JAVA class. The course emphasis is on <u>ADTs</u>.

#### Focus of the course

- In this course, we will study algorithms and ADTs for solving the most common computational problems: searching, sorting, indexing, etc.
- We will learn how to rigorously analyze an algorithm and describe its space and time complexity → is A1 always better than A2?
- We will learn how to adapt know algorithms and develop new ones.
- You will implement in JAVA variations of the algorithms to better understand them!

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# Algorithms and problem solving

Say you have a computational problem to solve

Is there an algorithm that solves it?
 → not always! Example: the halting problem.

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- Is there an efficient algorithm that solves it?
- → not always! Example: packing problem.
  Is my algorithm the best possible algorithm?
- → not necessarily! Example: sorting in  $O(n^2)$
- What is the best algorithm we can develop?
   → sorting takes Ω(*n*log*n*) time and Ω(*n*) space.

## Easy problems, hard problems

- Over the past 50 years (and especially the last 30 years), many algorithms for a wide variety of computational tasks have been developed
- A classification of hard and easy problems has also been developed, together with formal tools to prove what is their complexity and how they are related to each other.
- → Equivalence classes of *complexity*   $\Omega(n)$  – linear;  $\Omega(nlogn)$ ;  $\Omega(n^2)$  – quadratic;  $\Omega(n^k)$  – polynomial;  $\Omega(2^n)$  – exponential;  $\Omega(2^n)$  doubly exponential
  - unsolvable!  $(2^{2^n})$  = exponential,  $(2^{2^n})$  doubly expo

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	SPACE	Т	I M	Е
		Best	Worst	Average
Bubble	n	n	$n^2$	$n^{2}/2$
Sort		one pass	n passes	n/2 passes
Merge	$n \log n$	$n \log n$	n log n	n log n
Sort				
MergeS • Numb	ort: er of leve	els: $2^l = n$	$\rightarrow l = \log_2$	$2^{n}$

### Other types of algorithms and analyses

Up to now, you have studied exact, deterministic algorithms. There are other types as well:

- <u>Randomized algorithms</u>: makes random choices during execution: pick a random element from an array instead of the first one → minimize the chances of always picking a bad one!
- · Probabilistic analysis for randomized algorithms
- <u>Approximation algorithms</u>: instead of finding an optimal solution, find one close to it → bin packing.

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### Course topics (1)

- Techniques for formal analysis of asymptotic algorithm complexity with recurrence equations
- Techniques for solving recurrence equations: substitution, recursion-tree, master method.
- · Proving upper and lower bounds
- Sorting, in-depth: merge sort, quick sort, counting sort, radix sort, bucket sort.

#### Course topics (2)

- Common ADTs and their algorithms: heaps, priority queues, binary trees, AVL trees, Red-Black trees, B-trees.
- · Huffman codes, hash tables, hash functions
- Graph algorithms: Breadth-First Search, Depth-First Search, Shortest path algorithms, Minimum Spanning Trees, Strongly Connected Components.
- Union-Find of sets (time permitting).

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### Programming skills

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- Selected topics in JAVA
- Learn how to choose and implement ADTs Design and program a medium size project: the bookstore
- Learn how to use a debugger

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### Style of the lectures

- Algorithms and ADTs are described at a higher level, in *pseudo-code*, not in JAVA.
- We assume you know how to program by now, so you can turn an algorithm and an ADT into a JAVA program.
- More abstract and rigorous thinking: formal proofs of complexity, proofs of algorithm correctness.

